
APPROXCALIPER: A PROGRAMMABLE FRAMEWORK FOR APPLICATION-AWARE NEURAL NETWORK OPTIMIZATION

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ABSTRACT

To deploy compute-intensive neural networks on resource-constrained edge systems, developers use model optimization techniques that reduce model size and computational cost. Existing optimization tools are *application-agnostic* – they optimize model parameters solely in view of the neural network accuracy – and can thus miss optimization opportunities. We propose **ApproxCaliper**, the *first programmable framework for application-aware neural network optimization*. By incorporating application-specific goals, ApproxCaliper facilitates more aggressive optimization of the neural networks compared to application-agnostic techniques. We perform experiments on five different neural networks used in two real-world robotics systems: a commercial agriculture robot and a simulation of an autonomous electric cart. Compared to Learning Rate Rewinding (LRR), a state-of-the-art structured pruning tool used in an application agnostic setting, ApproxCaliper achieves $5.3\times$ higher speedup and $2.9\times$ lower GPU resource utilization, and $36\times$ and $6.1\times$ additional model size reduction for the two evaluated benchmarks, respectively.

1 INTRODUCTION

Many emerging edge applications combine multiple neural network (NN) models (which extract actionable information from sensor data such as RGB, LIDAR, audio, and GPS) together with other computations to achieve end-to-end goals. However, deep learning workloads are often compute- and power-intensive, which makes it challenging to deploy these models on resource-constrained edge compute devices with tight constraints on power, weight, size and production costs (Pedersen et al., 2006; Kim et al., 2010). An important opportunity, however, is that the applications exhibit a significant amount of *application-level error resilience*: reducing an individual component’s accuracy is acceptable if it has minimal *observable impact on the end-to-end quality of the application*.

Application-level error-resilience manifests in many different domains that use NNs, including autonomous navigation systems, augmented and virtual reality (AR/VR) stacks, and real-time data analytics. For instance, in an autonomously navigating robot, a reduction in the accuracy of the NN

perception component may not adversely affect the navigation quality, due to the error resilience in the control components. Similarly, we found that for a real-time data analytics application (corn stem counting using object detection), the final stem counts are minimally affected by locationing errors in the object detection component.

Currently, application developers can reduce the costs of NN models with various NN-specific optimization techniques such as pruning, quantization, weight compression, and low-rank factorization (Sainath et al., 2013; Han et al., 2016; Anwar et al., 2017; Frankle & Carbin, 2019; Hubara et al., 2017; Swaminathan et al., 2020; Ruan et al., 2021; Xu et al., 2021; Venkataramani et al., 2019). These techniques optimize a neural network with the goal to *maintain the same accuracy as the original model*. They have proven effective in many scenarios where the NN *is* the entire application. However, using NN optimization techniques naïvely for composite edge applications misses the rich opportunity to take advantage of the application-level resilience. Instead, it conservatively constrains the optimization levels to retain the accuracy of the original network, even when the constraint is not required to satisfy the application’s end-to-end QoS (Quality of Service) goal.

Our key insight is to incorporate the application-level error resilience in the optimization process, which allows relaxing the accuracy of NN components, yielding more aggressively optimized models and less costly execution. Application-aware optimization can provide several times more speedup

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and often more than an order of magnitude less memory consumption compared to application-agnostic techniques. These improvements make it possible to deploy compute-intensive NN models on resource-constrained edge systems, as we will demonstrate in this paper.

1.1 ApproxCaliper

We develop ApproxCaliper, the *first application-aware neural network optimization framework*. It is application-aware in that it uses a developer-specified application-level QoS goal for tuning. For instance, for an autonomous robot that uses neural networks for visual perception, a developer can specify an application-level QoS goal to autonomously navigate without collisions for a given distance. ApproxCaliper encodes this QoS goal as constraints under which it relaxes NN accuracy with approximation techniques to gain higher performance benefits.

Tuning the accuracy-vs-performance tradeoffs for neural networks deployed as components in applications is both complicated and time-consuming. Tuning is complicated because it searches across many low-level system- and NN-specific parameters with complex mutual interactions, and their impacts vary across different applications. For instance, for a control system that uses predictions from multiple NN components, errors in one component may affect how much error can be tolerated from other NNs, before quality of control decisions becomes unacceptably low. Tuning is time-consuming because the search space is often intractable, and empirically evaluating each configuration to measure application-level QoS can be expensive (e.g., running a robot in a field). Thus we need to guide the search toward the configurations that are likely to yield profitable tradeoffs.

To reduce the complexity and cost, our novel optimization algorithm starts from the observation that the acceptability of a configuration in the application-level tradeoff space depends on the error levels in all NN components. We thus *reduce* the problem of searching the end-to-end application’s QoS space to searching the local spaces of NN errors measured by NN-specific error metrics. Our algorithm navigates the NN error space with statistical error injection procedure that varies the level of error in each NN component, and uses the error injection results in the NN space to direct the end-to-end QoS optimization.

We present a two-phase optimization approach with an *online* (on-device) error calibration phase and an *offline* model tuning phase. Our novel **error calibration algorithm** uses statistical error injection to identify valid regions in the NN error space (i.e., those that contain the configurations that lead to acceptable application-level QoS) and separate them from the invalid regions. We show that this technique can guide the **model selection and tuning phase** (that makes use of one or more off-the-shelf application-agnostic NN optimization techniques) towards configurations that maximize the given objective while satisfying the error constraints.

ApproxCaliper can automatically tune multiple NN components jointly to select an optimized model variant for each component. It can also simultaneously tune for the choice of model variant and value of NN-specific performance metrics, such as model frames per second (FPS) if given by the developer, to optimize *system-level* goals such as resource utilization. ApproxCaliper provides an easy-to-use programmable interface for the developer inputs, such as QoS and error metrics.

1.2 Summary of Results

We evaluate two *real-world* autonomous cyber-physical systems, **CropFollow** and **Polaris-GEM** with five different NN architectures used for visual perception tasks (detailed in §2.2 and §2.3). For both systems, ApproxCaliper discovers significant room for relaxing NN accuracy while maintaining application-level QoS. For CropFollow, ApproxCaliper co-tunes two different NN models in the application, and achieves $5.3\times$ higher speedup and $36\times$ greater model size reduction compared to Learning Rate Rewinding (LRR), an application-agnostic state-of-the-art structured pruning algorithm. For Polaris-GEM, ApproxCaliper co-tunes for model FPS and pruned model variants (two main factors that affect the QoS of this application), and achieves $2.9\times$ lower GPU resource utilization and $6.1\times$ greater model size reduction compared to LRR.

For CropFollow, these performance improvements allowed us to run the full system on a single \$45 Raspberry Pi4. This compares favorably to the \$129 Jetson Nano (2023 prices), the cheapest device to deliver necessary performance with application-agnostic pruning (LRR). Our work has led Earthsense, CropFollow’s manufacturer ([Earthsense, 2020](#)), to consider lower cost alternatives for computing hardware.

1.3 Contributions

- We propose ApproxCaliper, the first programmable framework that optimizes neural network approximations in an *application-aware* manner. It captures how errors and performance of NN components in an application interact and affect the application-level QoS.
- We present a novel two-phase neural network model optimization strategy, with an error calibration phase and a model optimization and selection phase, which achieves higher end-to-end performance improvements compared to traditional empirical autotuning.
- Our evaluation on the end-to-end software stacks of two real-world cyber-physical systems shows that ApproxCaliper provides significantly higher improvements compared to application-agnostic tuning approaches.

ApproxCaliper is available at <https://github.com/uiuc-arc/approxcaliper>.

2 BACKGROUND AND MOTIVATION

We consider an application that includes one or more neural networks, and must achieve a design goal captured by a specified quality-of-service (QoS) metric. The goal of our work is to enable and simplify the use of aggressive optimizations that relax component-level semantics, such as NN inference accuracy, to the maximum extent possible while ensuring the QoS goal is met. We first define terminology used throughout the paper (§2.1), and then describe the two evaluated cyber-physical applications (§2.2 and §2.3).

2.1 Preliminaries and Terminology

Configuration is an assignment of a *possibly optimized model variant* (e.g., a pruned neural network with specific pruning fractions) to each NN component in the application, and (optionally) NN performance parameters such as the FPS (frames per second) at which the NN processes inputs (e.g., images).

Application-level QoS is an application-specific metric defined by a real-valued function for a specified configuration (the “QoS Evaluator”), along with a lower-bound value for the desired application quality (the “QoS Target”). This function should quantify how well the application delivers on its desired goals. For example, for an autonomous mobile robot, a relevant QoS metric for navigation quality is the time the robot travels before requiring human intervention, e.g., due to a collision.

Valid and Invalid Configurations. A configuration is *valid* if it meets the QoS target ($QoS \geq QoSTarget$), and is *invalid* otherwise ($QoS < QoSTarget$).

Autotuning is a design space exploration technique that uses heuristic techniques to find configurations that maximize a given objective function, while satisfying user-specified constraints. Since autotuning is a *heuristic search* performed over (usually) intractably large search spaces, it may not discover globally optimal configurations.

2.2 CropFollow Autonomous Navigation System

We evaluate a state-of-the-art commercial agriculture robot called *TerraSentia*, obtained from EarthSense (EarthSense, 2020), used by clients for high-throughput phenotyping and a variety of other agriculture tasks. The robot is equipped with an autonomous vision-guided navigation system named *CropFollow* (Sivakumar et al., 2021) used for *row-following* navigation through fields of crops.

CropFollow’s goal is to navigate the robot through the center line of a (possibly curved) crop row. It contains a number of components that collaborate to keep the robot on its intended path, as shown in Figure 1:

- *Heading / distance prediction NNs.* 2 ResNet-18 NNs take 320×240 RGB images as input and estimate the heading angle θ and distance-to-edge d of the robot. θ is the angle of the robot’s direction relative to adjacent crop rows. $d \in [0, 1]$ is the ratio between the robot’s distance

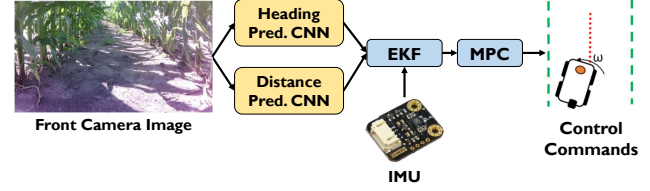


Figure 1: CropFollow navigation system workflow.

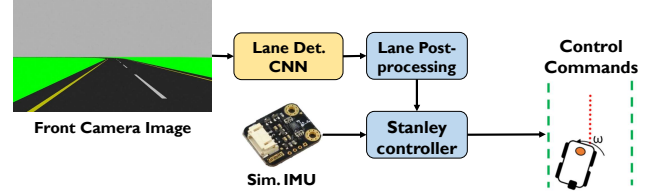


Figure 2: Polaris-GEM vehicle simulator workflow.

to the left crop row and the total row width.

- *Extended Kalman Filter (EKF).* EKF fuses (θ, d) predictions with measurements of linear and angular velocities and accelerations from an *Inertial Motion Unit* (IMU) to refine these predictions.
- *Model Predictive Controller (MPC).* MPC uses refined pose estimations from EKF to compute the angular velocity commands to be applied over the next few decision intervals, to keep the robot travelling on its intended path.

2.3 Polaris-GEM Vehicle Simulator

Polaris-GEM is a Gazebo-based simulation of an *autonomous lane-following*, commercially-sold electric cart, Polaris GEM e2 (Salfer-Hobbs & Jensen, 2020). The original simulator used GPS-based perception, but we modified it for vision-based perception using LaneNet (Neven et al., 2018), a state-of-the-art lane detection network. Figure 2 shows the components of Polaris-GEM, which include:

- *Lane Detection Network.* A LaneNet (Neven et al., 2018) with a VGG-16 backbone takes a 512×256 RGB image (from Gazebo-simulated front camera) and produces 2 outputs: a Boolean mask $B : 512 \times 256$ and an embedding tensor $E : 4 \times 512 \times 256$. B distinguishes lanes from the background; E distinguishes the lanes from each other.
- *Lane Post-processing.* The post-processing module combines the masks (B, E) with a clustering algorithm and finds each lane as a cluster of pixels. It then fits a *polynomial curve* through the pixels of each lane, and eventually converts these curve equations into heading and distance estimates (θ, d) (similar to CropFollow).
- *Stanley Controller.* A Stanley controller (Thrun et al., 2006) uses (θ, d) estimates and current velocity (from Gazebo-simulated IMU) to compute a steering angle and guide the vehicle back to the center.

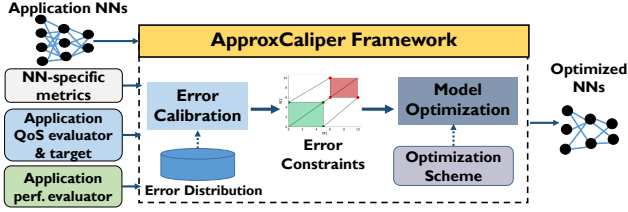


Figure 3: ApproxCaliper High-level Workflow

3 APPROXCALIPER FRAMEWORK

Figure 3 shows the workflow of the ApproxCaliper framework. At a high-level ApproxCaliper takes as input (1) NN models to optimize, (2) NN-specific metrics that are used to quantify the output error of the NN models (used for error calibration analysis), (3) a developer-provided QoS evaluator and QoS target, and (4) a developer-provided application performance evaluator, and uses these to perform application-aware optimizations on the NN models. To reduce the cost of tuning and improve the quality of configurations, ApproxCaliper performs optimization in two phases: (1) An *error calibration phase* (§3.2) that evaluates empirically how the end-to-end application QoS is affected by accuracy degradation of the NN components in the application pipeline, and (2) A *model tuning and selection phase* (§3.3) that optimizes the NNs based on the application’s error constraints computed by the calibration phase.

First, we discuss the high-level intuition of our approach, and next, the algorithmic details of the error calibration and model tuning phases in ApproxCaliper. In §3.4, we discuss how developers can use the ApproxCaliper interface to optimize neural networks in an application-specific manner.

3.1 Intuition for our Two-phase Tuning Approach.

Motivation. Empirical autotuning is *computationally expensive* because (1) it usually requires many tuning iterations to achieve good results, and (2) each empirical evaluation can be expensive; for instance, for CropFollow, empirical evaluation can be expensive in terms of both time and human resources because the *TerraSentia* robot needs a human observer for potential manual interventions.

ApproxCaliper’s two-phase tuning approach achieves higher speedups and model footprint improvements in the same tuning time budget as traditional empirical tuning. Systematically quantifying the error constraints before the tuning phase allows for filtering invalid configurations (unacceptably low QoS), and helps direct the search towards configurations that more likely has high speedups.

Goal of the Error Calibration Phase. The purpose of error calibration is to learn the extent to which the accuracy of NN components can be reduced without violating end-to-end application-level QoS targets. This is achieved by statistical error injection into NN outputs and empirical evaluation of the application QoS for a limited number of times. The injected errors are quantified using one or more tradi-

tional error metrics per NN, such as accuracy, precision, or any custom function. These error metrics $M_j, 1 \leq j \leq N$ define a bounded N -dimensional *error constraint space*. Figure 4 shows an example error constraint space with two error metrics $M1$ and $M2$. The error constraint space captures how *simultaneous* changes in the error metrics affects the end-to-end QoS. Error calibration partitions this space into three disjoint regions: **valid** (QoS \geq QoSTarget, shown in green) **invalid** (QoS $<$ QoSTarget, shown in red) and **unvisited** (unknown QoS, shown in white).

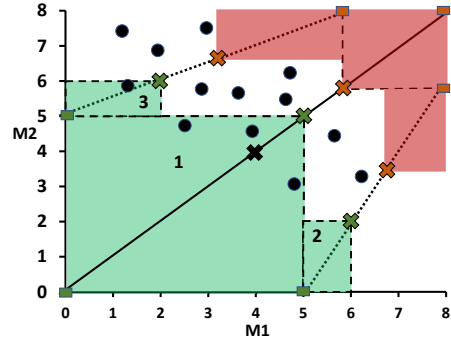


Figure 4: Example shows how the error calibration algorithm partitions the 2-dimensional error space into *valid* (green) and *invalid* (red) configuration regions. $M1$ and $M2$ are error metrics. Valid regions marked number 1, 2, 3 are created in the first 3 iterations, respectively. The green crosses show the MVP (maximal valid points) and red crosses show the MIP (minimal invalid points). The black dots show configurations searched on the boundary of the valid and unvisited regions.

Goal of the Model Optimization and Autotuning Phase.

The model autotuner uses heuristic search techniques to navigate the configuration space and *filters* away (1) invalid region (red region) configurations, and (2) valid region (green region) configurations with low error metric values. Configurations with lower error are *not* desirable since *a lower error means less opportunity for optimization*. We refer to valid configurations with high error metric values as *high potential* since a higher metric value indicates a higher error slack, and hence more optimization opportunity. *High potential* configurations are likely found close to the boundary of the valid and unvisited region, as this area includes the highest error values but still produces valid QoS. In Figure 4, the black dots in the green and white regions show the configurations searched in the model tuning phase. The unvisited (white) region is included in the search since it *potentially* includes valid configurations (has unknown QoS). There are no visited configurations on the bottom left of Figure 4, since points with low error metric values are *not* high potential configurations.

3.2 Error Calibration Phase

The error calibration phase uses artificial error injection to add varying levels of errors to NN outputs, and measures the impact on the end-to-end application-level quality. Next,

we describe the key inputs to the error calibration phase, the error calibration algorithm, and our approach to error injection in NN outputs.

Developer Input #1: Baseline Neural Networks. Developers specify one pretrained NN model per NN component to use for error injection. These are the baseline models with no approximation. It is preferred that developers specify models with high accuracy since it gives the highest margin for error injection.

Developer Input #2: Neural Network Metrics. The ApproxCaliper interface provides developers with a flexible way to specify task-specific NN error metrics, which is important since different NN tasks use different metrics. Developers can use a predefined error metric or provide a custom function $ErrorMetric(Y, G)$, where Y is the output of the NN model after error injection and G is the ground truth. Developers can also specify a performance metric such as DNN throughput, and ApproxCaliper can analyze the combined impact of NN compute performance (e.g., FPS) and prediction error (e.g., accuracy) on end-to-end QoS. The interface allows specifying multiple metrics (e.g., precision and recall) per NN that capture different aspects of the error. For each metric, users also need to provide *lower and upper bound* values as the range for error injection.

The error calibration algorithm assumes that *all the metrics are monotonic with the same directionality*, i.e., a higher metric value is always more desirable than a lower value. This monotonicity assumption is satisfied by most common metrics such as classification accuracy, F1 score, PSNR (peak signal-to-noise ratio), etc. If a metric m is monotonic but in the opposite direction, one can instead use $-m$.

Developer Input #3: End-to-end QoS Evaluator. Developers provide the QoS evaluator and the QoS target via the ApproxCaliper interface. The error calibration algorithm uses this QoS evaluator to measure the impact of NN errors on the end-to-end QoS. This function should initialize the application, run the application for some time / iterations, and return the end-to-end QoS.

Output. The output is an N -dimensional *error constraint space* that captures the effect of increasing NN error on the application QoS. The error constraint space is a space of the N metrics (Input #2). The lower and upper bounds of each metric collectively define two N -dimensional points $M_{lb} = (M_{lb,1}, \dots, M_{lb,N})$ and $M_{ub} = (M_{ub,1}, \dots, M_{ub,N})$ and an N -dimensional *box* between them that forms the overall search space. We refer to a single or an union of more N -dimensional boxes as a *region*. The algorithm partitions the search space into valid (green) and invalid (red) region, effectively finding the boundary between these two regions. Figure 4 shows an example of a 2-dimensional error constraint space where $M_{lb} = (0, 0)$ and $M_{ub} = (8, 8)$.

Algorithm 1: Error Calibration Algorithm.

```

1 Inputs:
2   • baselineNNs: pretrained NNs, one per NN component
3   • qosEvaluator: function that evaluates app-level QoS
4   • qosTarget: QoS target to satisfy
5   • lowerBound, upperBound: thresholds for metrics
6   • errorDistrib: error distribution for sampling errors
7   • maxDiagEvals: maximum evaluations per diagonal
8   • totalEvals: total number of evaluations
9 Output: validRegion, invalidRegion, unvisitedRegion
10 Function errorCalibrate
11   fullRectangle = Rectangle(lowerBound, upperBound);
12   rectQueue = PriorityQueue([fullRectangle]);
13   nEvals = 0;
14   while not rectQueue.empty() and nEvals < totalEvals do
15     rectangle = rectQueue.pop();
16     diag = rectangle.getDiagonal();
17     for rEvals = 0 to maxDiagEvals do
18       if nEvals ≥ totalEvals then break;
19       errorInjectedNNs = errorInject(baselineNNs,
20         errorDistrib, diag.midPoint);
21       qos = qosEvaluator(errorInjectedNNs);
22       if qos ≥ qosTarget then
23         diag = Diagonal(diag.midPoint, diag.MIP);
24         diag.MVP = diag.midPoint;
25       else
26         diag = Diagonal(diag.MVP, diag.midPoint);
27         diag.MIP = diag.midPoint;
28       nEvals += 1;
29       validRegion ∪ = DominatedRect(diag.MVP);
30       invalidRegion ∪ = DominatedRect(diag.MIP);
31       rectQueue.push(rectangle.getSubRectsToVisit());
32   unvisitedRegion = fullRectangle − validRegion −
33     invalidRegion;
34   return validRegion, invalidRegion, unvisitedRegion;

```

3.2.1 Error Calibration Algorithm

Algorithm 1 shows the error calibration algorithm. The core idea is to recursively divide the search space into smaller rectangles and search for boundary points (representing configurations) on the diagonal of each rectangle. The algorithm exploits *domination relation* in the space to efficiently infer validity of rectangles. If a point P is evaluated as valid, the algorithm infers the rectangle with lower or equal error than P in all metrics $R_{L;P} = \{Q \mid \forall i. Q_i \leq P_i\}$ as **valid**. We say point P *dominates* all points $Q \in R_{L;P}$, and P is the *highest* point of $R_{L;P}$. Conversely, if P is invalid, the rectangle $R_{U;P}$ with higher or equal error than P is **invalid**, P is *dominated* by all points $Q \in R_{U;P}$, and P is the *lowest* point of $R_{U;P}$. By this definition, each rectangle has a unique lowest point and a unique highest point.

For each rectangle, we perform a binary search (Lines 16-27) on its *diagonal*. For each point to evaluate, the error injection procedure adds error into NNs' outputs (Line 19); see §3.2.2 for details on error injection. The algorithm traverses this diagonal to find a *pair of boundary points*: a *maximal valid point* (MVP) and a *minimal invalid point* (MIP). MVP is the highest point on the diagonal that evaluates as valid and MIP is the lowest invalid point. The rectangle

dominated by MVP is added into the valid region (Line 28), and the rectangle that dominates MIP is added into the invalid region (Line 29). Then the algorithm computes rectangles to visit next based on the coordinates of MVP and MIP (Line 30). The gap between MVP and MIP also creates an unvisited rectangle (usually small). The volume of this rectangle is controlled by the number of evaluations done per diagonal (`maxDiagEvals`); a higher number of evaluations per diagonal increases analysis time but reduces the size of the unvisited rectangle. The algorithm finishes when the queue of rectangles is empty or the number of QoS evaluations reaches `totalEvals`.

Example. Figure 4 illustrates *three* outer loop iterations of the algorithm. Assuming two error metrics, $M1$ and $M2$, the first iteration traverses the diagonal between $(0, 0)$ (lowest metric values) and $(8, 8)$ (highest metric values). It first evaluates the midpoint $(4, 4)$ (shown as a black cross). Given $(4, 4)$ is found as a *valid point* a new higher midpoint $(6, 6)$ is evaluated. $(6, 6)$ is found as an invalid configuration and hence the search proceeds to evaluate a new midpoint $(5, 5)$. Assuming three evaluations on the diagonal (`maxDiagEvals` = 3), $(5, 5)$ is found to be the diagonal’s MVP and $(6, 6)$ is found as the MIP, which are used to create the dominating rectangular green (valid) region and red (invalid) region, respectively. Subsequent iterations create further green and red rectangles – green rectangles labelled 2 and 3 are created in 2nd and 3rd iteration, respectively.

3.2.2 Error Injection in NN outputs

The error injection algorithm injects error to NNs’ outputs as $Y = X + \varepsilon$, where X is the output of the non-approximate NN, Y is the output after error injection, and $\varepsilon \sim \mathcal{D}(p)$ is a sample from an error distribution with parameters p . For given error values (a point x chosen by the error calibration algorithm), the error injection algorithm searches for the distribution parameter values that produce an output error close to the given x . This step does not require expensive empirical evaluation and has negligible overhead.

Selecting an Error Distribution. ApproxCaliper *automatically* selects a distribution that best mimics the errors that occur with an approximation technique (e.g., with low-rank factorization). Given a pretrained NN, a calibration dataset, and approximation techniques, ApproxCaliper generates approximated NN variants and evaluates them on the calibration dataset to measure the output errors. ApproxCaliper then finds a fittest one from a set of predefined parametric distributions, by computing the Bayesian information criterion (BIC) for each distribution on the output errors and selecting the one with the lowest BIC. For floating-point outputs, ApproxCaliper chooses from Gaussian, log-normal, exponential, and Student-T distribution; for integer outputs, it evaluates binomial, Poisson, and logarithmic distributions. Users can easily add more error distributions by implementing a sampling function usually with a few lines of code.

3.3 Model Tuning and Optimization

In the model tuning phase, ApproxCaliper searches for *configurations* that minimize the given performance objective while satisfying the application-level QoS target. A configuration contains choices of optimized NN variants generated by approximation techniques (described later). It may also include NN-specific performance metrics (e.g., model FPS); this allows ApproxCaliper to co-tune for NN performance and error. Each configuration corresponds to a point (black dots in Figure 4) in the error constraint space.

To explore the search space more efficiently, ApproxCaliper uses the error constraint space to skip empirical evaluations for (1) configurations in the invalid region, and (2) low-potential configurations in the valid region. We now describe how the autotuning search decides if a configuration lies within a low-potential valid region. The error calibration phase yields a valid region as a union of rectangles. each with one vertex at $(0, 0)$. Moving the MVP vertex of each rectangle by $k\%$ towards $(0, 0)$ creates a smaller rectangle, which we treat as a low-potential valid region. Here, $k\%$ is a user-configurable hyperparameter. For example, in a rectangle between $(0, 0)$ and $(1, 1)$, the rectangle between $(0, 0)$ and $(0.95, 0.95)$ is low-potential when $k\% = 5\%$. ApproxCaliper skips navigating configurations in these low-potential rectangle regions.

Figure 4 shows how ApproxCaliper only searches for *high potential* configurations in these regions. This helps *steer the search* away from both low-potential (too conservative) and known invalid configurations. Our approach ensures that costly empirical evaluations are only spent on configurations that are likely to provide high improvements.

NN Approximation Techniques in ApproxCaliper. ApproxCaliper currently supports two existing approximation techniques (which can be applied in combination): (1) structured pruning based on *Learning Rate Rewinding* (LRR) (Renda et al., 2020) and (2) low-rank factorization (or LR factorization) based on (Tai et al., 2016). Developers can also incorporate new approximation techniques (e.g., perforated convolutions (Figurnov et al., 2015)) with the ApproxCaliper interface.

Structured pruning works iteratively: in each iteration, it removes a fraction of filters with the lowest L1 norm from each convolution layer, and retrains the model to recover some of the lost accuracy. Each iteration produces smaller and more efficient models with (usually) lower accuracy, creating a tradeoff space of models to choose from.

LR factorization decomposes each (convolution and matrix multiply) weight tensor into 2 lower-rank tensors. For instance, a 2D convolution layer with weights of shape $(C_{out}, C_{in}, H_k, W_k)$ can be decomposed into 2 convolution layers with weights of shape $(R, C_{in}, 1, W_k)$ and $(C_{out}, R, H_k, 1)$ where the free parameter R controls the rank of the decomposition. A lower R means more ap-

```

import approx_caliper as ac
# Load NN models; supports Pytorch and ONNX models
heading_nn, distance_nn = ac.load_model("resnet18_h.onnx"), ac.load_model("resnet18_d.onnx")
nns = [heading_nn, distance_nn]
trainset = ac.load_dataset("cropfollow_data/", "cropfollow_labels.json")
# Define metrics for measuring the error of each NN's output; to be used in error calibration.
metrics = [ac.ErrorMetric(heading_nn, ac.ll_error), ac.ErrorMetric(distance_nn, ac.ll_error)]
# Use predefined Structured Pruning method to compress the NNs
# Prune 20 levels with each level pruning 20% of the weights
structured_pruner = ac.nn_approx.StructuredPruner(n_steps=20, prune_fraction=0.2)
# Fits the errors of the optimization technique to an error distribution -- e.g., Gaussian, Bernoulli
error_dist = ac.find_error_distribution(structured_pruner, nns, trainset)
# User provides method to evaluate end-to-end application quality and application performance
qos_eval, perf_eval = CropFollowQoSEvaluator(), CropFollowPerfEvaluator()
# error_calibrate interface invokes the Error Calibration phase -- computes error constraints
constraints = ac.error_calibrate(
    nns, error_model, metrics, qos_eval, qos_target={"collision": 0}, iters=25)
# optimize input NNs using the given optimization scheme (structured pruner)
optimized_nns = ac.optimize(structured_pruner, constraints, nns, trainset, qos_eval, perf_eval)

```

Figure 5: Example of using the ApproxCaliper interface with the NN components in the CropFollow autonomous navigation stack.

proximation, less computation, and less accuracy. Similar to pruning, we apply LR factorization iteratively (not proposed in the original work (Tai et al., 2016)), where ranks of weight tensors are reduced in each iteration. Additionally, in the first iteration, each layer is decomposed into two layers. In further iterations, only the ranks of weight tensors are reduced, and no more layer splitting is performed. We make this choice to avoid an explosion of layers, which can hurt compute performance.

Autotuning to Search Profitable Configurations. The NN variants produced by the approximation techniques and NN-specific performance metrics (if any) together create a large search space of configurations on which an exhaustive approach is intractable. To make the search feasible, we use OpenTuner (Ansel et al., 2014), a library for building custom autotuners. In addition to the QoS evaluator, autotuning also uses the application performance evaluator that developer provided to ApproxCaliper.

3.4 ApproxCaliper Programmable Interface

ApproxCaliper is developed as a Python library with an easy-to-use API. Figure 5 presents an example of how the ApproxCaliper interface is used to optimize the heading and distance prediction NNs in the CropFollow autonomous navigation stack. The key interface functions in the example are described and explained within the comments.

As Figure 5 shows, using ApproxCaliper’s interface to optimize a new application requires only a few lines of code. The application QoS evaluation and performance evaluator are the only functions that developers need to implement. These evaluators run the application multiple times to compute the QoS and measure the performance. Since application test suites usually include such scripts, it requires minimal additional effort in most cases. Further, developers need to specify the number of runs used in error calibration

phase and model optimization phase. This is a common practice in existing autotuning works, as automatic stopping criteria (e.g. stop on convergence) are rarely satisfied.

4 EXPERIMENTAL METHODOLOGY

Optimization Goals and Constraints. We apply ApproxCaliper on **CropFollow** to optimize its 2 NN models simultaneously, maximizing the application-level FPS without introducing collisions. *The QoS target* is that the robot should have 0 collisions with the row boundaries in a 100m run in corn fields at the Illinois Autonomous Farm. The QoS evaluator prompts for the number of total collisions, which a human observer observes and manually inputs after each run, since the robot has no automatic collision detection mechanism. *The optimization goal* FPS is a proxy for latency, and is relevant for autonomous navigation systems because feedback control systems have *minimal FPS requirements* (Falanga et al., 2019; Anwar & Raychowdhury, 2020) to function correctly. FPS improvements enable execution on low-end compute devices which would otherwise not provide minimal FPS.

Similarly, we apply ApproxCaliper on **Polaris-GEM** to jointly optimize model FPS and model approximation. ApproxCaliper searches for an optimized (e.g., pruned) NN model and the FPS that the NN component runs at, to minimize GPU utilization without introducing lane departures. Running the model at a lower FPS reduces GPU utilization as the process sleeps between frames, freeing up GPU cycles. *The QoS target* is the robot should make 0 departures from the current lane in a 506 meter run in simulation. *The optimization goal*, GPU utilization, is a known proxy (Fan et al., 2007) for power usage; we don’t report power numbers since there is no easy way to precisely measure power on the target GPU, an Nvidia Quadro P5000.

Approximation Techniques Setup. We implemented structured pruning and LR factorization based on the original papers – (Renda et al., 2020) for pruning and (Tai et al., 2016) for LR factorization. For both techniques, we set up ApproxCaliper to use a fixed number of iterations each removing an additional 20% filters or ranks. We apply pruning with 20 iterations for NNs in CropFollow and 12 iterations for LaneNet (as the lane detection quality decreases significantly after that point). We apply LR factorization to LaneNet with also 12 iterations. We name as a *prune level* the output model of each iteration and label it from 1 to 20 (or 12) inclusive, and 0 is the unpruned baseline.

Error Calibration and Model Tuning Setup. There are 63 candidates for each of the two NN components in CropFollow, creating a total of $63 \times 63 = 3969$ combinations. Brute force search is infeasible since each empirical *field evaluation* takes 4-5 minutes. The same holds true for Polaris-GEM which has 2730 configurations and each run takes 5-6 minutes. While we had performed more than 700 hours of field experiments to refine our algorithms, we limit the tuning to 50 navigation runs (~ 5 hours). Of those, we use 20 runs in error calibration phase and 30 in model optimization phase. We compare the result against 50 unguided (without ApproxCaliper) autotuning runs using Opentuner. For the $k\%$ parameter that decides the size of the high-potential valid region we use 5%.

Tuning Space and Tuning Time Budgets. As shown above, there are 3969 configurations for CropFollow; for Polaris-GEM, the autotuner searches over 26 model candidates for LaneNet and 105 FPS values (chosen between 0 to 10.5 at 0.1 intervals), with total 2730 configurations. The LaneNet FPS is limited by the clustering algorithm (see §2.3) which runs at a max of 10.5 FPS. Like CropFollow, each evaluation is expensive since it involves a 506-meter long simulator navigation run that consumes 5-6 minutes, and we maintain an ~ 5 hour tuning time budget for 50 runs. The fractions of configurations searched in unvisited and valid regions are set to 75% and 25%, respectively. For the valid region, 5% of the area closest to the boundary is included in the search ($k\% = 5\%$).

Neural Network Specific Error Metrics. For both NNs in CropFollow, we use *standard deviation of error* as the error metric in error calibration, because pruned models mostly have zero-centered errors (confirmed by zero-mean Gaussian distribution that ApproxCaliper found). In Polaris-GEM, the quality of lane detection is measured by *lane detection accuracy*, a quantity between 0 (worst) and 1 (best): $Acc = \sum_{image} \frac{C_{im}}{S_{im}}$, where C_{im} is the number of correctly detected lanes in an image, and S_{im} the number of lanes in ground truth. A lane is correctly detected if the average distance between its detected points and the ground-truth points is less than 20 pixels (the same threshold used in the TuSimple challenge (Zhou, 2018)).

Application-agnostic Baseline. As baselines for comparison, we apply pruning using LRR (Renda et al., 2020) or LR factorization using the technique in (Tai et al., 2016) to all the candidate neural network architectures with the constraint to *retain the same accuracy as the original model*, and pick the most efficient pruned variant from this set as our baseline. This represents an intelligent use of today’s state-of-the-art model optimization approaches, which accounts for manual selection of neural network architecture and optimized variants, *but does not exploit application resilience to increased inference error*. For instance, for Polaris-GEM, LaneNet-DarkNet prune level 1 (20% weights pruned) is selected as the baseline since it is the most efficient pruned model that retains the original model accuracy of the unpruned LaneNet-DarkNet model, and is more compute-efficient than any of the LaneNet-VGG16 optimized model variants with equivalent accuracy.

Model Architectures and Training. For CropFollow, we evaluate three NN architectures for both heading and distance prediction: ResNet-18 (He et al., 2016) (default), SqueezeNet-v1.1 (Iandola et al., 2016), and DarkNet (Redmon & Farhadi, 2018). We use NNs pretrained on ImageNet (Deng et al., 2009) and fine-tune with 25K corn row images. For Polaris-GEM, we evaluate LaneNet with two backbones: VGG-16 (Simonyan & Zisserman, 2014) (default) and DarkNet (Redmon & Farhadi, 2018). We fine-tune pretrained backbones on the TuSimple dataset (Zhou, 2018) with 3600+ images. We use a 4:1 split between training and validation sets for both datasets.

Error Distributions. ApproxCaliper finds zero-mean Gaussian $\mathcal{N}(0, \sigma^2)$ as the closest error distribution for the NNs in CropFollow (using the `ac.find_err_distribution` routine – §3.4). The mean is 0 since the errors are mostly zero-centered; the variance σ is a parametric value that is varied in error injection. In Polaris-GEM, ApproxCaliper finds Bernoulli distribution $\mathcal{B}(p)$ for the Boolean mask and zero-mean Gaussian distribution $\mathcal{N}(0, \sigma^2)$ for the embedding tensor (see §2.3 for these outputs).

5 EVALUATION

In our experiments, we consider the following questions:

RQ1: Does ApproxCaliper’s application-aware pruning provide more benefits than today’s practice of application agnostic pruning (retaining original model accuracy)?

RQ2: Does the ApproxCaliper error calibration framework identify opportunities for relaxing NN accuracy requirements without impacting the end-to-end QoS?

RQ3: Do the error calibration results guide ApproxCaliper to better tune the NN components than “*unguided tuning*”? Unguided tuning is in-field autotuning without considering the error constraint space computed by the calibration phase, i.e., this requires exploring configurations anywhere within the search space.

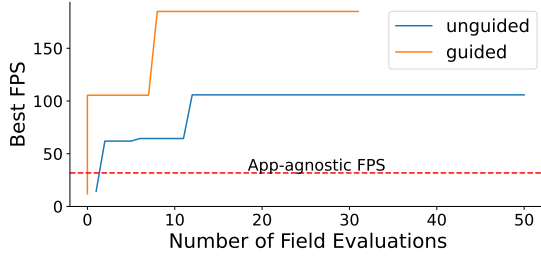


Figure 6: CropFollow tuning result. Graph shows how the performance in FPS (higher is better) of the best configuration evolves with increasing field evaluations. ApproxCaliper guided and unguided tuning is compared with LRR app-agnostic baseline.

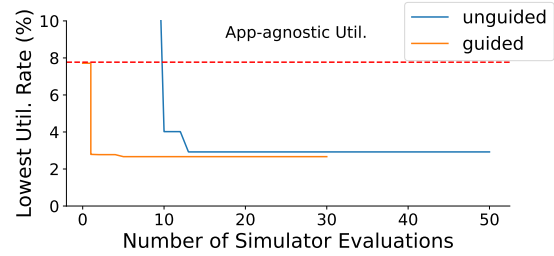


Figure 7: Polaris-GEM tuning result. Graph shows how the GPU utilization rate (lower is better) of the best configuration evolves with increasing simulator evaluations. ApproxCaliper guided and unguided tuning is compared with LRR app-agnostic baseline.

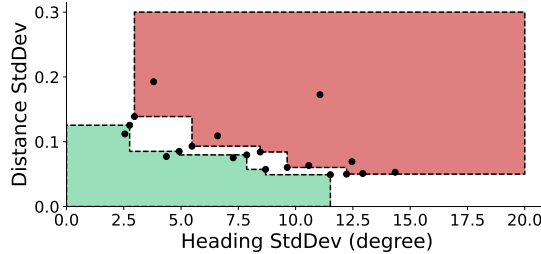


Figure 8: Error constraint space for CropFollow. It captures the interaction of errors in the heading model (x-axis) and the distance model (y-axis). Green region is the valid QoS region, red region is the invalid QoS region, and white regions are unvisited. The black dots on the figure show field evaluations.

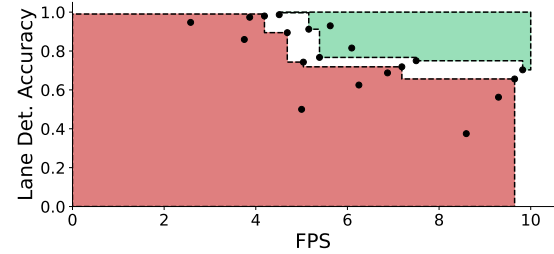


Figure 9: Error constraint space for Polaris-GEM. It captures the interaction of FPS (x-axis) and the errors in the LaneNet model (y-axis). Green region is the valid QoS region, red region is the invalid QoS region, and white regions are unvisited. The black dots on the figure show simulator evaluations.

RQ4: Do the valid and invalid regions obtained by calibration correspond to the real-world separation between acceptable and unacceptable configurations?

RQ5: Does ApproxCaliper’s application-aware optimization provide performance improvements with other approximations such as LR factorization?

5.1 Application-aware vs Application-agnostic Pruning

To answer RQ1, we compare the best pruning configurations for CropFollow and Polaris-GEM, selected by 3 strategies, all using LRR: (1) guided tuning with ApproxCaliper, (2) unguided autotuning with ApproxCaliper, and (3) the application-agnostic pruning baseline. We focus on LRR (i.e., structured pruning) here because it gave dominant results over LR factorization.

For CropFollow, Figure 6 shows how the performance (FPS) of the best configuration (found until that point) evolves with the increasing number of tuning iterations. Application-agnostic pruning using LRR gives a flat line (31.8 FPS) since this approach simply uses the best performing pruned model for heading and distance predictions, and does not involve any further tuning in the field. Application-aware pruning using ApproxCaliper provides significantly higher FPS: unguided tuning provides an FPS of 105.8 (i.e., $3.3\times$ faster than application-agnostic pruning) and guided tuning provides 184.9 FPS (i.e., $5.8\times$ faster). These are dramatic speedups obtained with the same optimization techniques,

i.e., *purely by accounting for application-level quality goals*. Similarly, for Polaris-GEM, Figure 7 shows the GPU utilization rate of configurations, which decreases over the course of tuning. Using application-agnostic pruning on LaneNet achieves a GPU utilization of 7.77%. Unguided and guided application-aware pruning using ApproxCaliper reduces the utilization to 2.92% ($2.66\times$ reduction) and 2.67% ($2.91\times$ reduction) respectively.

5.2 Error Calibration using ApproxCaliper

To answer RQ2, we apply ApproxCaliper’s error calibration framework to identify how much error can be introduced to the NN predictions without affecting the navigation quality of CropFollow and Polaris-GEM. These experiments explain **how** ApproxCaliper achieves substantial overall gains.

Error Calibration Results on CropFollow. Figure 8 shows the error constraint space for CropFollow. Each of the 20 error calibration field evaluations are shown as black dots. Our key findings are:

- The heading model error in isolation (no errors in distance model) can be increased from 2.5 (baseline) to 11.5 degrees, without introducing collisions.
- Distance model error can be increased from 0.05 (baseline) to 0.13, without introducing collisions. In absolute terms, 0.13 is a large standard deviation of error since $0 \leq \text{distance} \leq 1$ (row center is 0.5).

- Errors can be simultaneously increased in both models. For instance, heading error and distance error can be simultaneously increased by $3\times$ and $1.6\times$, respectively, without introducing collisions.

Overall, these observations show that ApproxCaliper discovers *significant room for relaxing the accuracy*.

Error Calibration Results on Polaris-GEM. For Polaris-GEM, we study the *interplay of model FPS and lane detection accuracy*. We performed a similar analysis (and found similar insights) for CropFollow that we do not include for lack of space. Figure 9 shows the generated error constraint space. The key findings are:

- Higher FPS can counteract the effect of higher errors. As FPS increases from 4.5 to 9.8, lane detection accuracy can be reduced from 99.7% to 70.3%, without introducing any lane departures. Further investigation showed that, at high FPS, the effect of an erroneous prediction is short-lived since it enables more control actions per second.
- FPS and lane detection accuracy compensate for each other to a limited extent. No configuration with FPS below 4.5 or lane detection rate below 70% is feasible.

5.3 Guided vs. Unguided Tuning on CropFollow.

To answer RQ3, we compare guided and unguided tuning with ApproxCaliper.

Comparing Speedups. Figure 6 shows the model FPS achieved by guided and unguided tuning for CropFollow. Guided tuner provides a $1.76\times$ speedup (184.9 FPS vs. 105.8 FPS) over unguided tuning. Guided tuning also finds many more high-performance configurations. Across 30 field evaluations of guided tuning, it found 5 configurations that provided higher FPS than the unguided tuner’s best result (105.8 FPS) in 50 field evaluations.

Figure 7 shows the utilization rate achieved by guided and unguided tuning for the Polaris-GEM experiment. Guided tuning provides a $1.1\times$ speedup over unguided tuning (GPU utilization of 2.66% vs. 2.92%). In addition, guided auto-tuning discovers the best found configuration on only the second simulator evaluation, while unguided tuning didn’t find a single valid configuration (i.e., one with acceptable QoS) for the first 10 evaluations (hence the blue line starts at evaluation 10 in Figure 7).

Effectiveness of Guided Tuning. Guided tuning uses the error calibration result to filter out configurations in the invalid regions and less performant configurations that are not fully pushing the boundary of acceptable error. A large fraction, 82% (41/50) of configurations evaluated in our unguided tuning experiment for CropFollow, and 78% (39/50) of configurations for unguided tuning for Polaris-GEM would be filtered/skipped if the same configurations are considered using guided tuning (i.e., using the error constraint space from calibration phase). Guided tuning is more effective because it focuses more of the tuning budget on

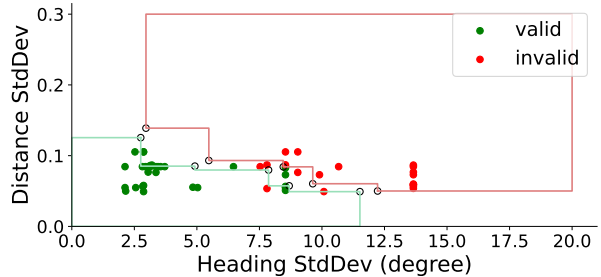


Figure 10: CropFollow: Configurations evaluated empirically in unguided autotuning (points) vs. error calibration regions used by guided autotuning (red and green polygons).

configurations that are not known to be (likely) invalid, and likely to be performant.

5.4 Testing the Configurations in the Wild

To evaluate RQ4, Figure 10 shows the 50 configurations evaluated in unguided tuning for CropFollow (Figure 6) overlaid on the error calibration results (Figure 8). We illustrate using unguided tuning since the configurations are more spread out across all 3 regions (valid, invalid, and undetermined regions) than guided tuning. Valid and invalid configurations are shown as green and red points respectively. *Only two of the 50 points are false positives* (red points in the green region), and there are no false negatives (no green points in the red region). The white region is unvisited and is expected to include both valid and invalid points. Similarly, for Polaris-GEM (figure not shown), we observe *only three false positives and no false negatives* out of 50 simulator evaluations for unguided tuning.

The results show that the valid/invalid regions found by the error calibration phase correspond well to the real-world separation between acceptable and unacceptable configurations. The few false positives we observe (e.g., red point in the green boundary region) are likely due to out-of-distribution errors, caused by networks being trained on different data (standard neural network training assumption).

5.5 ApproxCaliper with Low-rank Factorization

Our results so far used structured pruning since it provided a strictly better tradeoff (better accuracy and performance) compared to LR factorization. A key contribution of ApproxCaliper, however, is that it can make NN optimizations more effective by allowing them to be used more aggressively, even with reduced accuracy, by ensuring that the overall application use case meets its goals. Here we evaluate the LR factorization technique to show that these benefits of ApproxCaliper generalize beyond pruning. We generate 12 factorization levels of the LaneNet-VGG16 NN used in Polaris-GEM and evaluate the end-to-end QoS (lane departure situations) for each of the optimized model variants. For simplicity, we do not vary FPS and configure the FPS to its maximum of 10.5. If the model provides an FPS higher than the configured FPS of 10.5, artificial sleeps are added be-

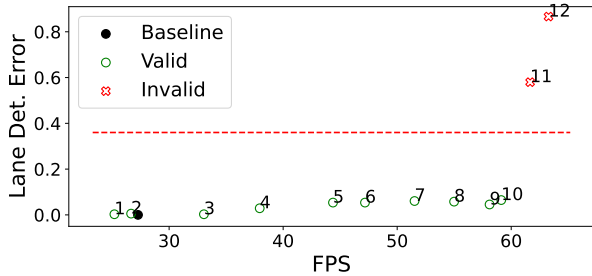


Figure 11: The compute performance (FPS) vs. lane detection error of low-rank factorized models. Green points have valid QoS, and red points have invalid QoS. The red dotted line shows error threshold (36.4%) above which configurations are invalid.

tween model invocations, to reduce GPU utilization. Hence, a higher model FPS enables lower GPU utilization. Figure 11 presents the different factorization levels laid out on an accuracy vs. performance tradeoff space.

The highest factorization level with acceptable QoS is level 10, which provides an FPS of 59.1, $2.2\times$ higher than factorization level 2, which is the most efficient model with error lower than (or equal to) the baseline. The key takeaway is that ApproxCaliper enables both LR factorization and LRR to deliver much higher benefits by considering the error slack in the application; we expect these benefits to extend to other accuracy-relaxing optimizations.

6 RELATED WORK

There is a long record of work on approximate computing approaches (Stanley-Marbell et al., 2020) that relax accuracy to improve application performance and programming systems for accuracy-aware optimization (Misailovic, 2022). We focus here on systems for optimization in deep learning.

Systems for Automatic Model Optimization. A major limitation of existing neural network optimization systems (Han et al., 2016; 2015; Zhu & Gupta, 2018; Frankle & Carbin, 2019; Anwar et al., 2017; He et al., 2017; Li et al., 2017; Molchanov et al., 2017; Hubara et al., 2017; Zhou et al., 2016; 2017; Zhu et al., 2017; Swaminathan et al., 2020; Sainath et al., 2013; Davis & Arel, 2014; Chen et al., 2017) is that they *tune NN models in isolation*, and unlike ApproxCaliper, do not exploit application-level error resilience. ApproxCaliper has complementary goals to these model optimization techniques. ApproxCaliper can use these techniques (e.g., pruning and low-rank factorization) much more aggressively – it relaxes model accuracy to the extent that application-level goals are not compromised.

Accuracy-aware ML Optimization Systems. While some automated model optimization systems (Tian et al., 2021; Sharif et al., 2019; 2021; Xu et al., 2020; 2021; Joseph et al., 2020) allow users to specify an acceptable accuracy loss specification (e.g., 1%, 2% loss) for optimization, these strategies are not *application-aware*. Instead, they consider the neural network to be the entire application, i.e., the NN error is the QoS loss. This work shows that application-

level error resilience often allows individual NN accuracy to be relaxed more aggressively to gain higher compute performance while satisfying end-to-end QoS goals. One important limitation of existing accuracy-aware optimization systems is the lack of mechanisms for jointly optimizing in the presence of simultaneous errors in multiple neural network components in the application (as ApproxCaliper does in §5.2). A second important limitation is that none of these systems can model the joint impact of NN’s accuracy and performance on application QoS. As our Polaris-GEM results show, the end-to-end QoS is not only dependent on NN accuracy: it can also be impacted by NN latency (FPS) and other application-specific parameters (§5.2). ApproxCaliper’s capabilities are broader than existing accuracy-aware optimization systems. It defines a programmable interface for computing application-specific error constraints, and can model error interactions across multiple NN components and between performance and accuracy.

7 DISCUSSION AND CONCLUSION

ApproxCaliper is the first programmable framework for application-aware neural network optimization. We present a novel approach for optimizing an application’s end-to-end QoS that reduces the search space to the error space of its neural network components. Our evaluations on autonomous cyber-physical systems show that application-aware optimization has tremendous potential in enabling compute-intensive ML models to run on edge hardware. Similar opportunities for approximation exist in AR/VR, data analytics, and robotic manipulation, and many others. Our preliminary results (not included) show that a stem counting data analytics workload and a eye-tracking based foveated rendering (Singh et al., 2023) also present significant opportunities for application-aware optimization. Beyond inherently approximate applications, we anticipate that ApproxCaliper’s error calibration can be generally used to quantify the level of error-resilience across various kinds of applications.

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